

Low-Distortion Signal Generation for Analog/Mixed-Signal IC Testing Using Digital ATE Output Pin and BOST

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Research Objectives

Objective

Low-Distortion Signal Generation

- For analog/mixed signal IC Testing
- High quality test signal

Approach

- Rectangular add/subtract method
- Proposed phase control method

Digital ATE + Simple analog circuit & BOST



No need expensive signal generator

ATE: Automatic Test Equipment

BOST: Built-Out Self-Test

Outline

- **Research Background**
- **Signal Generation Method**
- **Phase Shift Technique**
- **Circuit Configuration & Simulation**
- **Conclusion**

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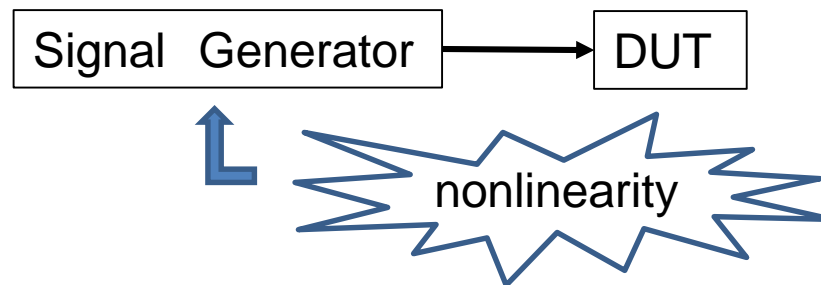
Research Background

- Testing analog ICs requires low distortion sinusoidal



Signal generator has nonlinearity

- Harmonic distortion caused
- Test accuracy deterioration



Objective _____

Low-Distortion Signal Generation at Low Cost

Problem of Our Previous Method

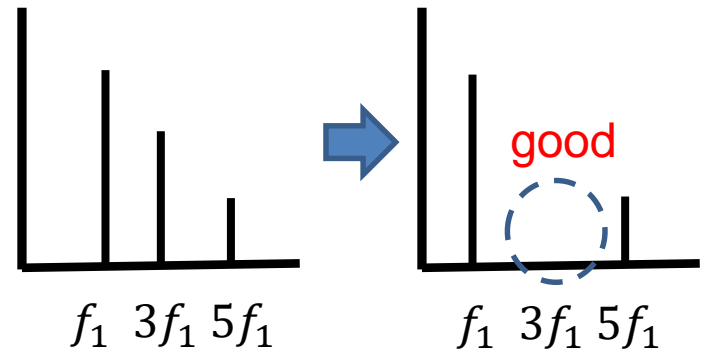
3rd harmonics suppression

Phase parameters

$$\varphi_1 = 2\pi \frac{\tau_1}{T}$$



3 rectangular add/subtract



Phase shift parameter

$$\tau_1 = \pm \frac{T}{6k}$$

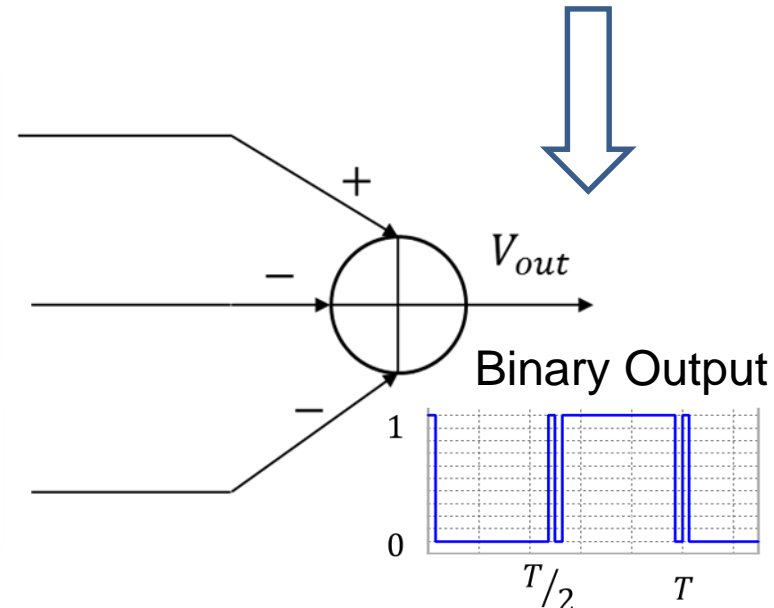
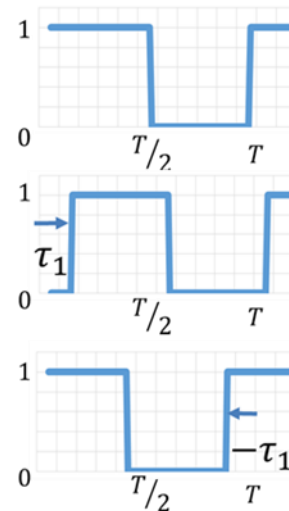
Phase shift parameter is simple



High resolution is not needed



Digital phase shift



- [1] M. Kawabata, et. al., "Low-Distortion Signal Generation for Analog/Mixed-Signal Circuit Testing Using Digital ATE", International Test Conference in Asia (Sept. 2017).

Problem of Conventional Method

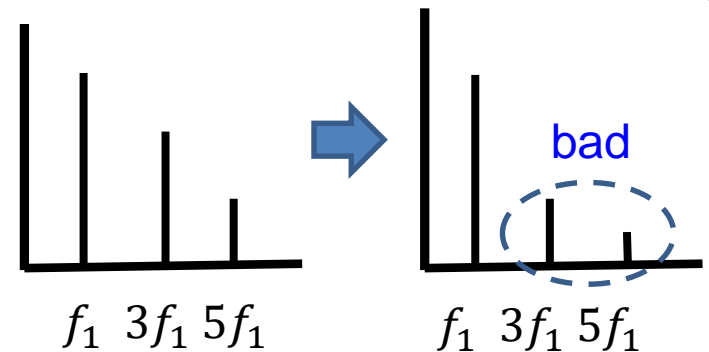
3rd & 5th harmonics suppression

Phase parameters

$$\varphi_1 = 2\pi \frac{\tau_1}{T}, \varphi_2 = 2\pi \frac{\tau_2}{T}$$



5 rectangular add/subtract



Phase shift parameter

$$\tau_1 = \frac{T}{2k\pi} \left(\cos^{-1} \left(\frac{1}{2} \left\{ 1 - 2 \cos \left(\frac{2k\pi}{T} \tau_2 \right) \right\} \right) \right)$$

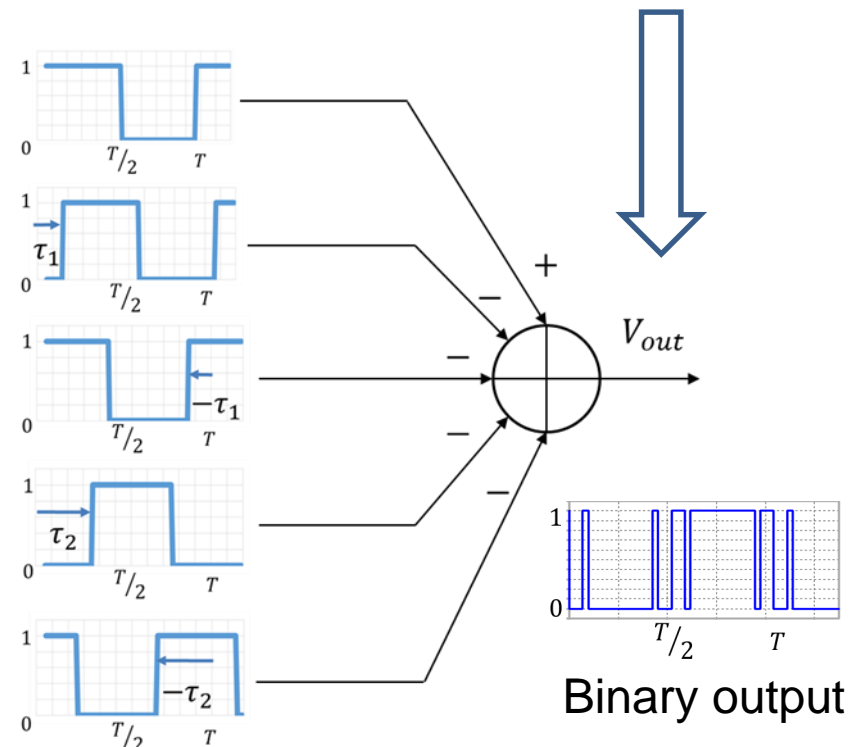
Phase shift parameter is complex



High resolution is needed



Analog phase shift



Outline

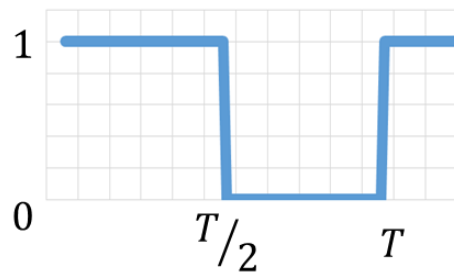
- Research Background
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Fourier Series Expansion

Duty 50% rectangular wave

$$f(t) = \begin{cases} 1 & \dots nT \leq t \leq (2n + 1)T/2 \\ 0 & \dots (2n + 1)T/2 < t \leq (n + 1)T \end{cases}$$

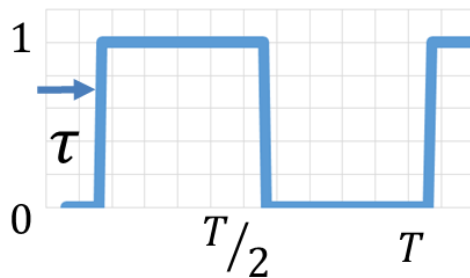
($n = 0, 1, 2, \dots$)



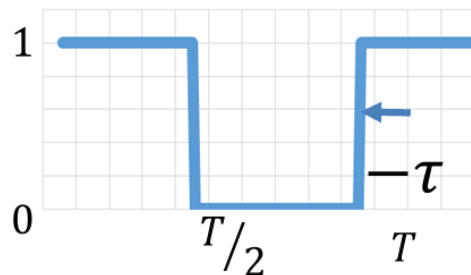
Fourier Series Expansion

$$f(t) = \frac{1}{2} + \sum_{m=1}^{\infty} \frac{2}{k\pi} \sin\left(\frac{2\pi}{T} kt\right)$$

($k = 2m - 1, m = 1, 2, \dots$)



$$f(t - \tau) = \frac{1}{2} + \sum_{m=1}^{\infty} \frac{2}{k\pi} \sin\left\{\frac{2\pi}{T} k(t - \tau)\right\}$$



$$f(t + \tau) = \frac{1}{2} + \sum_{m=1}^{\infty} \frac{2}{k\pi} \sin\left\{\frac{2\pi}{T} k(t + \tau)\right\}$$

Single Harmonic Suppression Method ^{10/26}

- Three rectangular waveforms add/subtract

$$V_{out} = f(t) - \{f(t - \tau_1) + f(t + \tau_1)\}$$

$$= -\frac{1}{2} + \sum_{m=1}^{\infty} \frac{2}{k\pi} \left\{ 1 - 2 \cos \left(\frac{2k\pi\tau_1}{T} \right) \right\} \sin \left(\frac{2k\pi}{T} t \right)$$

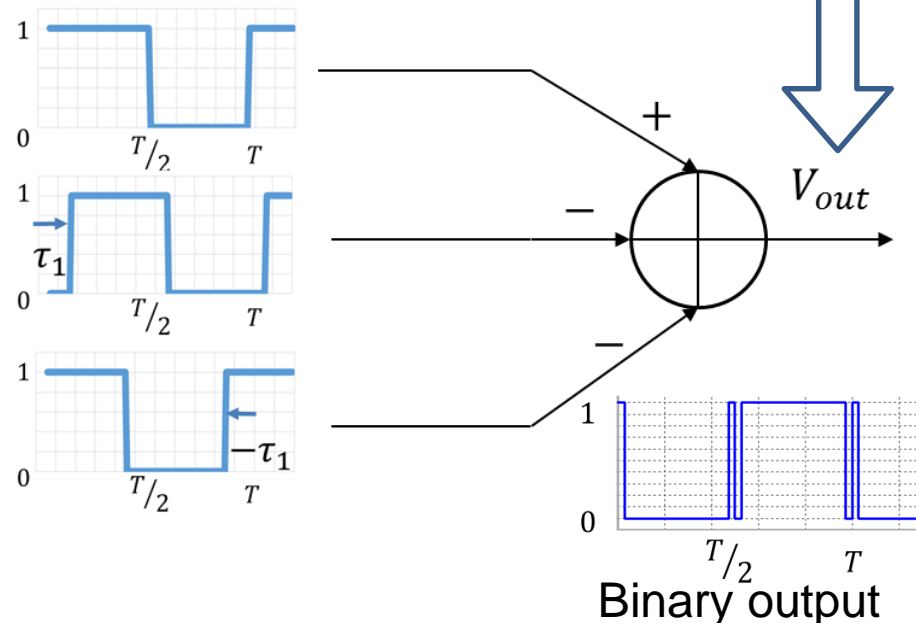
$$(k = 2m - 1, m = 1, 2, \dots)$$

- K-th HD suppression parameter

$$\frac{2}{k\pi} \left\{ 1 - 2 \cos \left(\frac{2k\pi\tau_1}{T} \right) \right\} \sin \left(\frac{2k\pi}{T} t \right) = 0$$

↓

$$\tau_1 = \pm \frac{T}{6k}$$



Multiple Harmonics Suppression Method

- Five rectangular waveforms add/subtract

$$V_{out} = f(t) - \{f(t - \tau_1) + f(t + \tau_1)\} - \{f(t - \tau_2) + f(t + \tau_2)\}$$

$$= -\frac{3}{2} + \sum_{m=1}^{\infty} \frac{2}{k\pi} \left\{ 1 - 2 \cos\left(\frac{2k\pi\tau_1}{T}\right) - 2 \cos\left(\frac{2k\pi\tau_2}{T}\right) \right\} \sin\left(\frac{2k\pi}{T}t\right)$$

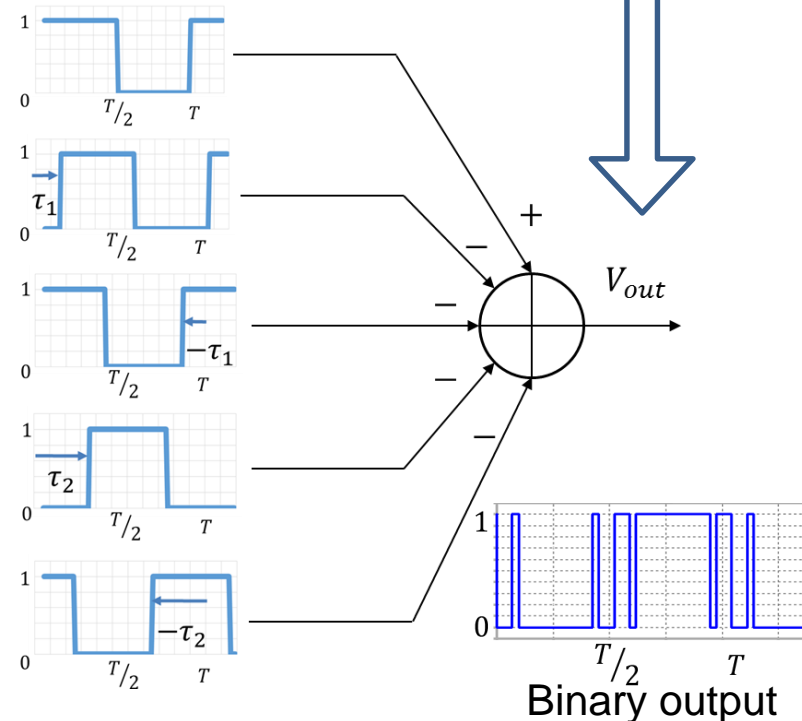
$$(k = 2m - 1, m = 1, 2, \dots)$$

- K-th HD suppression parameter

$$\frac{2}{k\pi} \left\{ 1 - 2 \cos\left(\frac{2k\pi\tau_1}{T}\right) - 2 \cos\left(\frac{2k\pi\tau_2}{T}\right) \right\} \sin\left(\frac{2k\pi}{T}t\right) = 0$$



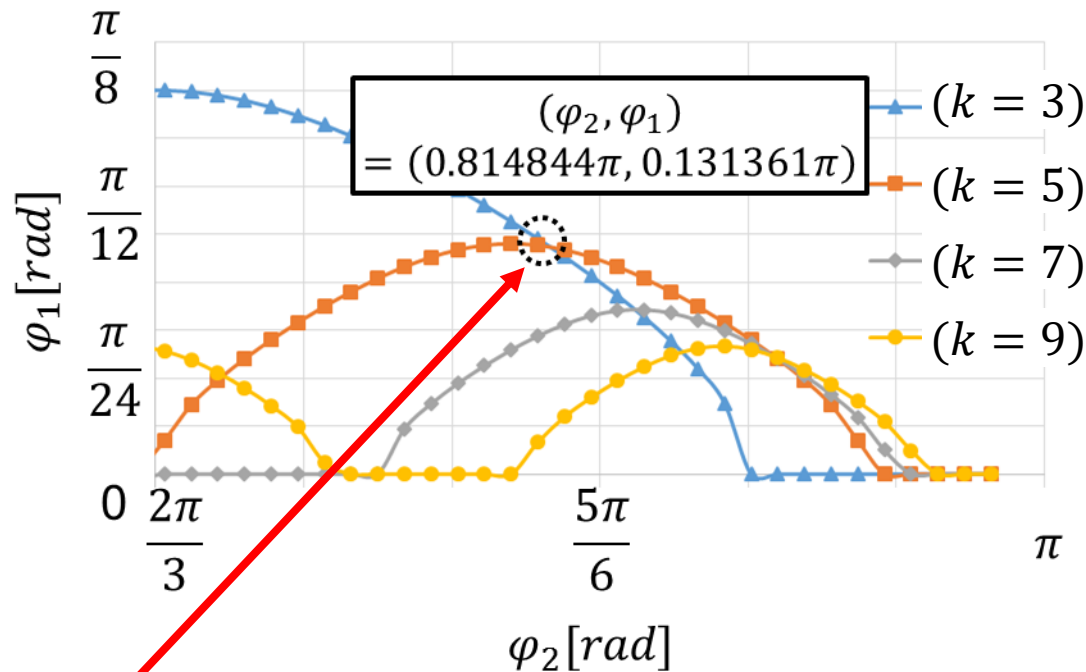
$$\tau_1 = \frac{T}{2k\pi} \left(\cos^{-1} \left(\frac{1}{2} \left\{ 1 - 2 \cos\left(\frac{2k\pi}{T}\tau_2\right) \right\} \right) \right)$$



Multiple Harmonics Suppression Parameter

$$\tau_1 = \frac{T}{2k\pi} \left(\cos^{-1} \left(\frac{1}{2} \left\{ 1 - 2 \cos \left(\frac{2k\pi}{T} \tau_2 \right) \right\} \right) \right)$$

$$\varphi = 2\pi \frac{\tau}{T} [\text{rad}]$$



Cross point  multi harmonics suppression parameter

 High quality needed

Outline

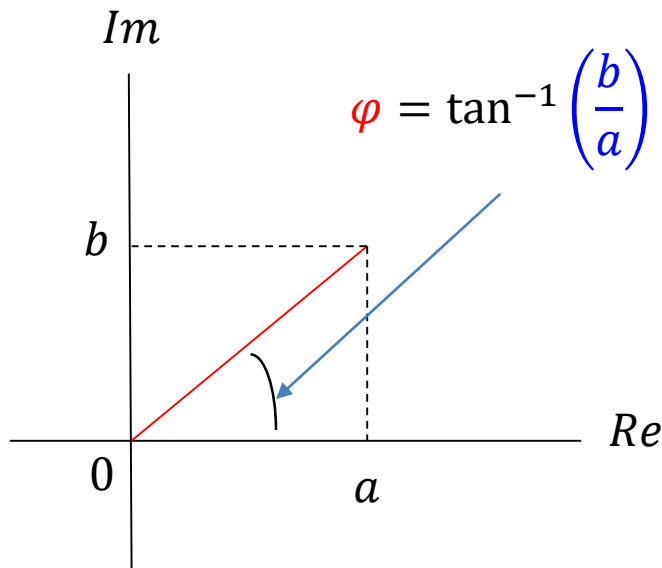
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Principle of Analog Phase Shift Technique

Formula of trigonometric function

$$a \sin(\omega t) + b \cos(\omega t) = \sqrt{a^2 + b^2} \sin(\omega t + \varphi)$$

$$\varphi = \tan^{-1} \left(\frac{b}{a} \right)$$

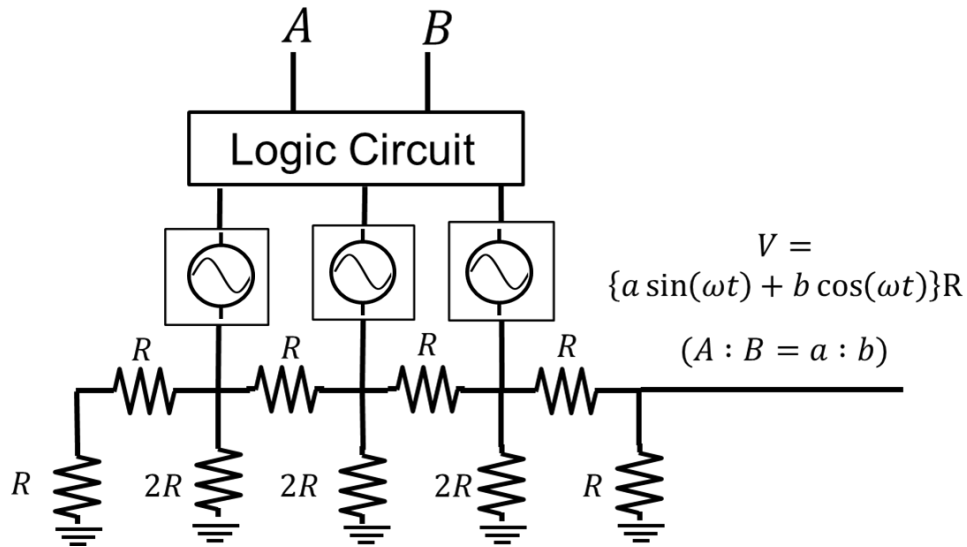


Control amplitude ratio $\frac{b}{a}$

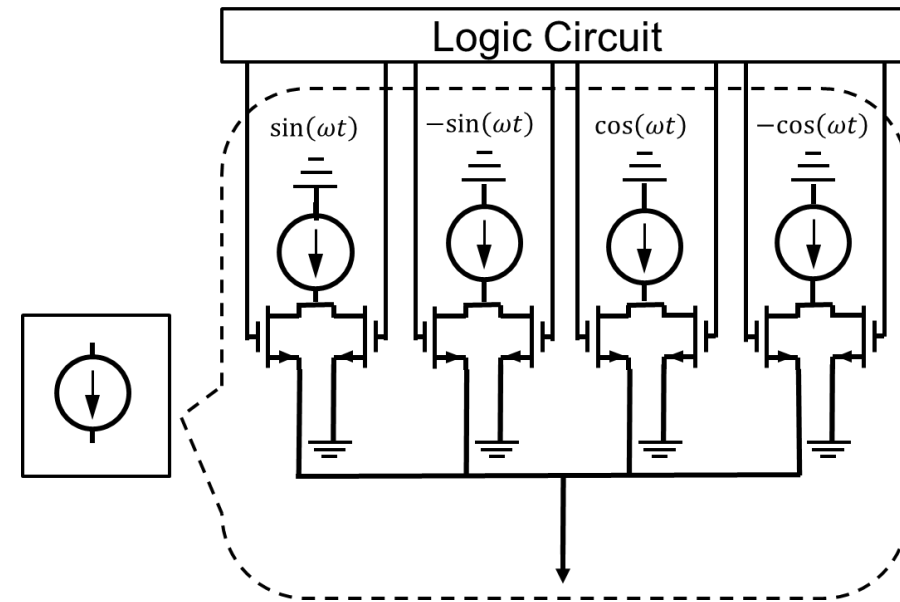


Control phase φ

Phase Control Circuit



R - 2R Ladder register
+
AC current source



Control current source by NMOS switch

Realize amplitude ratio A : B

Fractional Approximation Method

- Amplitude ratio $\frac{B}{A}$ of phase φ

$$\tan(20^\circ) = 0.363970 \dots \approx \frac{99}{273} = \frac{B}{A}$$

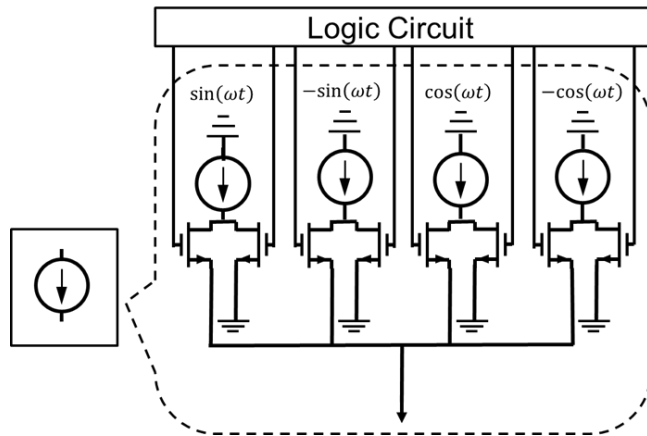
Fractional Approximation Method

$$3.14 \dots = 3 + \frac{1}{7.0625159} \approx 3 + \frac{1}{7} = \frac{22}{7}$$

$$3.14 \dots = 3 + \frac{1}{7 + \frac{1}{15.99593}} \approx 3 + \frac{1}{7 + \frac{1}{16}} = \frac{355}{113}$$

Using continued fraction  accurate amplitude ratio

Current Source Nonlinearity

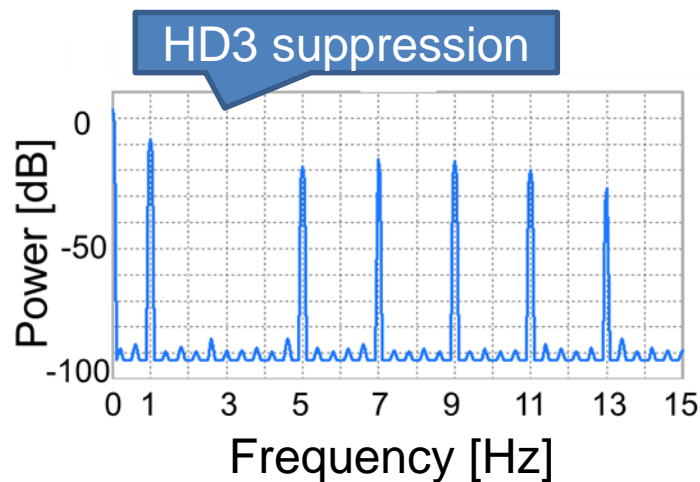


$$I = c_1 \sin \theta + c_3 \sin^3 \theta$$

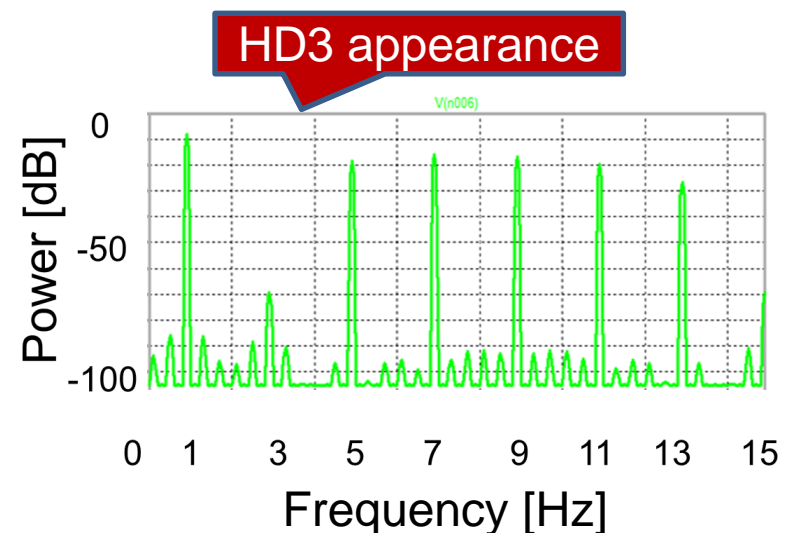
$$c_1 = 1, c_3 = -0.01$$

HD3 suppression case

linear



nonlinear



Amplitude Ratio Calculation

$$\begin{aligned}\frac{b}{a} &= -\frac{c_1 \sin(2\pi f_1 t + \theta) + c_3 \sin^3(2\pi f_1 t + \theta)}{c_1 \cos(2\pi f_1 t + \theta) + c_3 \cos^3(2\pi f_1 t + \theta)} \\ &= -\frac{c_1 + c_3 \sin^2(2\pi f_1 t + \theta)}{c_1 + c_3 \cos^2(2\pi f_1 t + \theta)} \tan(2\pi f_1 t + \theta)\end{aligned}$$

$$a_1 = 1, a_3 = -0.01, t = \frac{1}{9} [s], f_1 = 1 [Hz], \theta = 0 [^\circ]$$



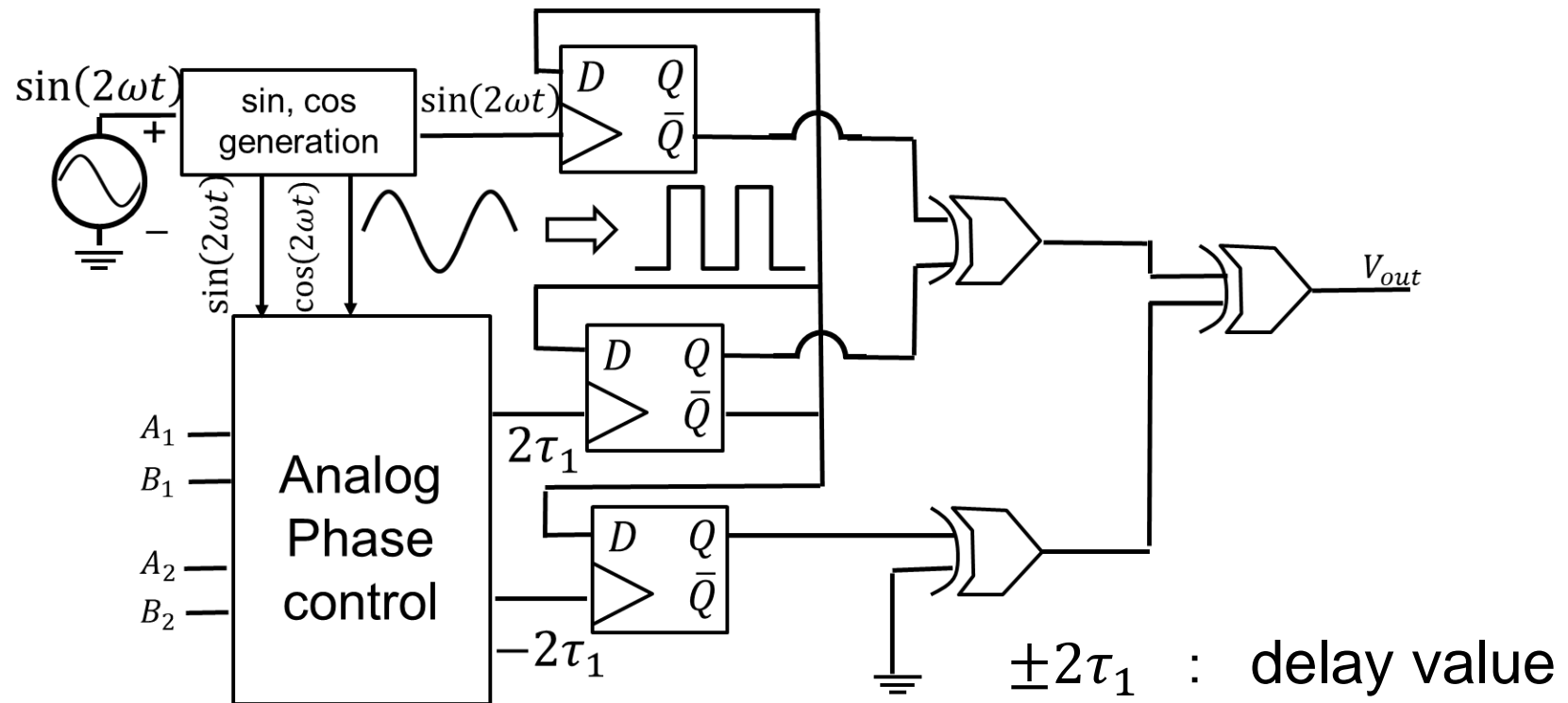
$$\frac{b}{a} = -\frac{1 - 0.01 \times \sin^2\left(\pm \frac{\pi}{9}\right)}{1 - 0.01 \times \cos^2\left(\pm \frac{\pi}{9}\right)} \tan\left(\pm \frac{\pi}{9}\right) = \mp 2.299560241 = \frac{\mp 522}{227}$$

Obtain appropriate amplitude ratio

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Duty50% Circuit Configuration

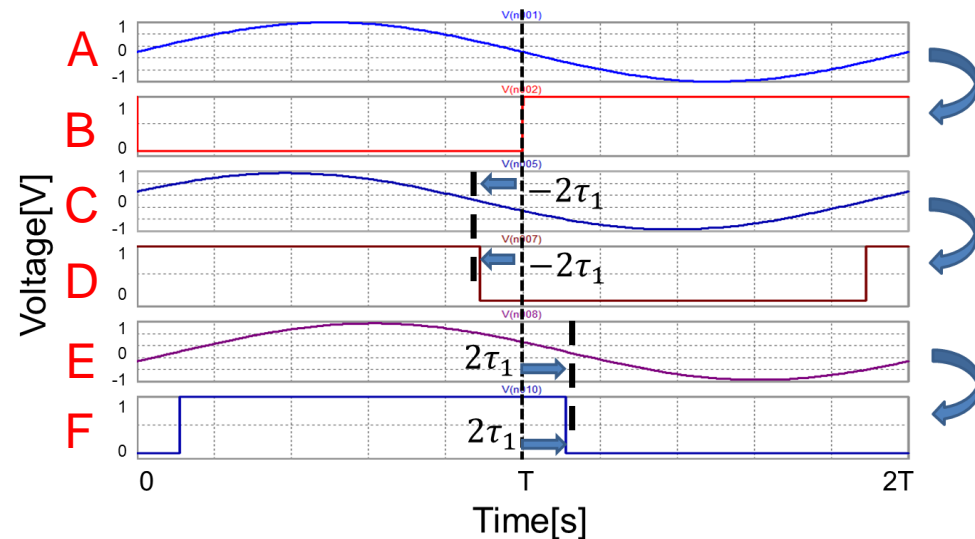
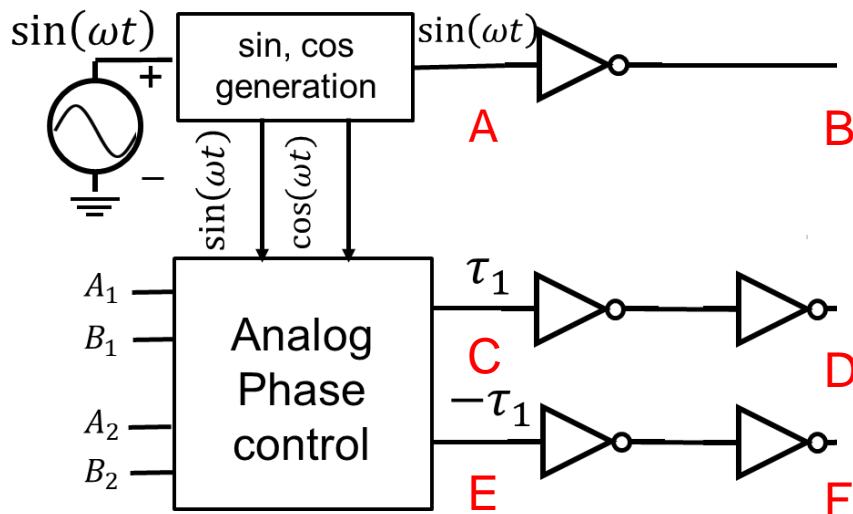


- Use a **frequency divider**
 - Guaranteed Duty 50%
 - Doubled phase and frequency
- Use **XOR** instead of opamp

From Sine to Rectangular Waveforms

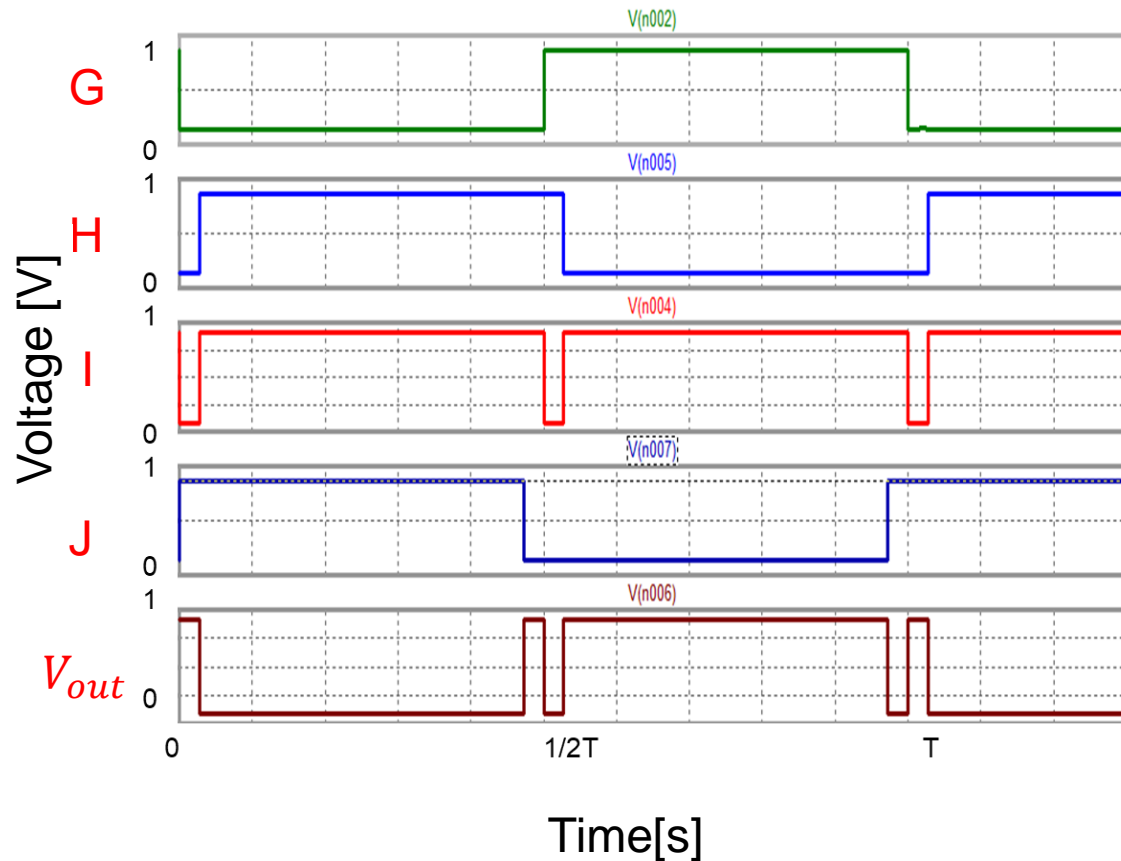
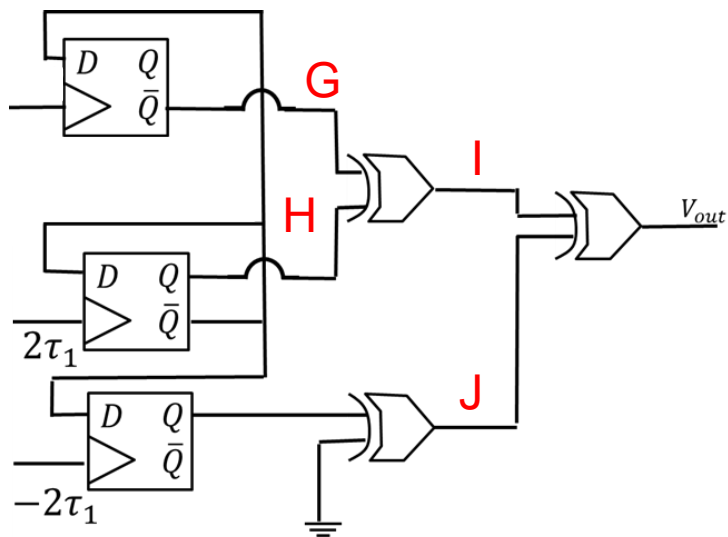
Sin wave \longrightarrow inverter \longrightarrow rectangular wave

Phase φ Binary change Phase φ



XOR Behavior

Binary output \rightarrow Express with logic circuit

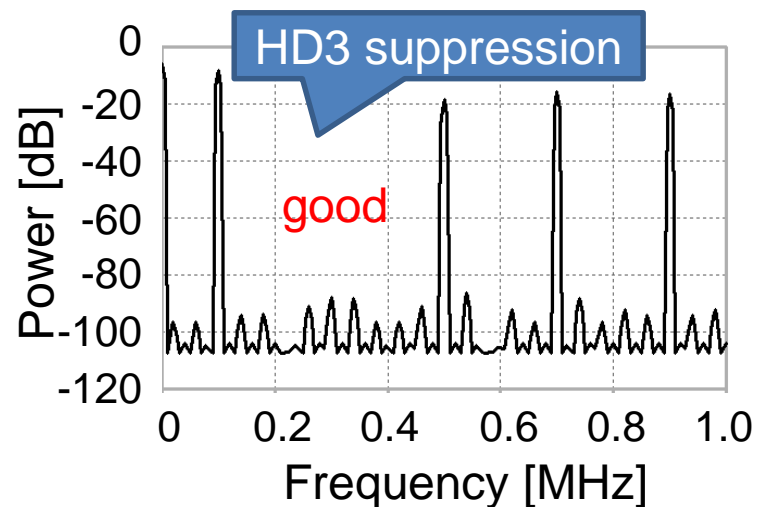
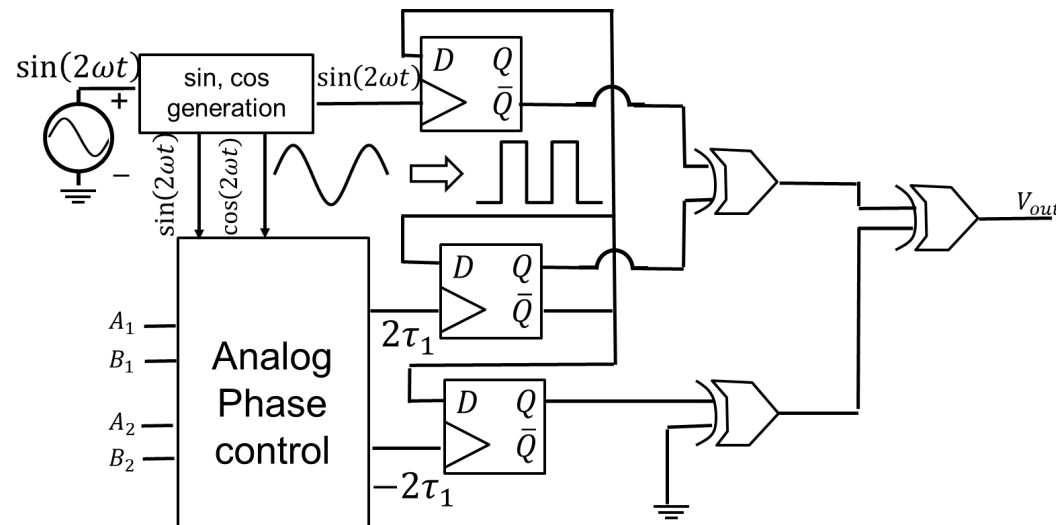


HD3 Suppression Simulation

Parameters

$$T/2 = 5 [\mu s], c_1 = 1, c_2 = -0.1, c_3 = -0.01$$

$$2\tau_1 = \frac{10}{9} [\mu s], \frac{b_1}{a_1} = \frac{587}{689}, \frac{b_2}{a_2} = \frac{350}{361}$$



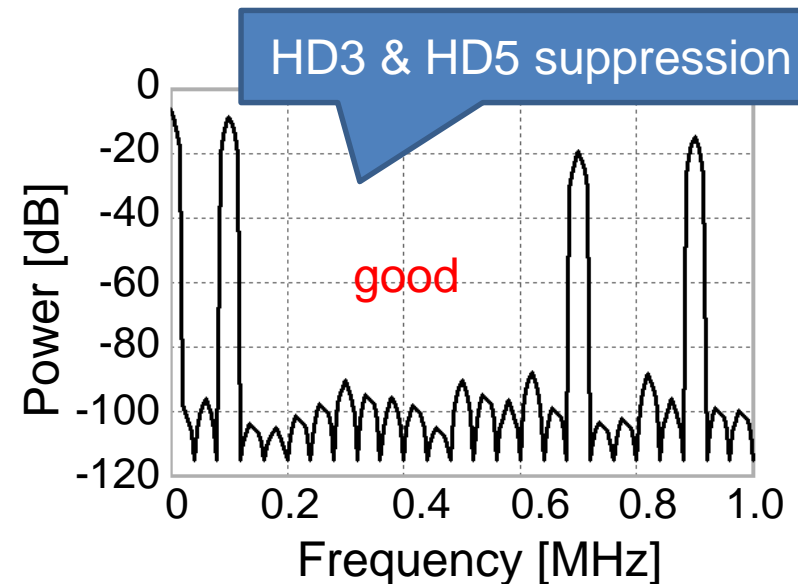
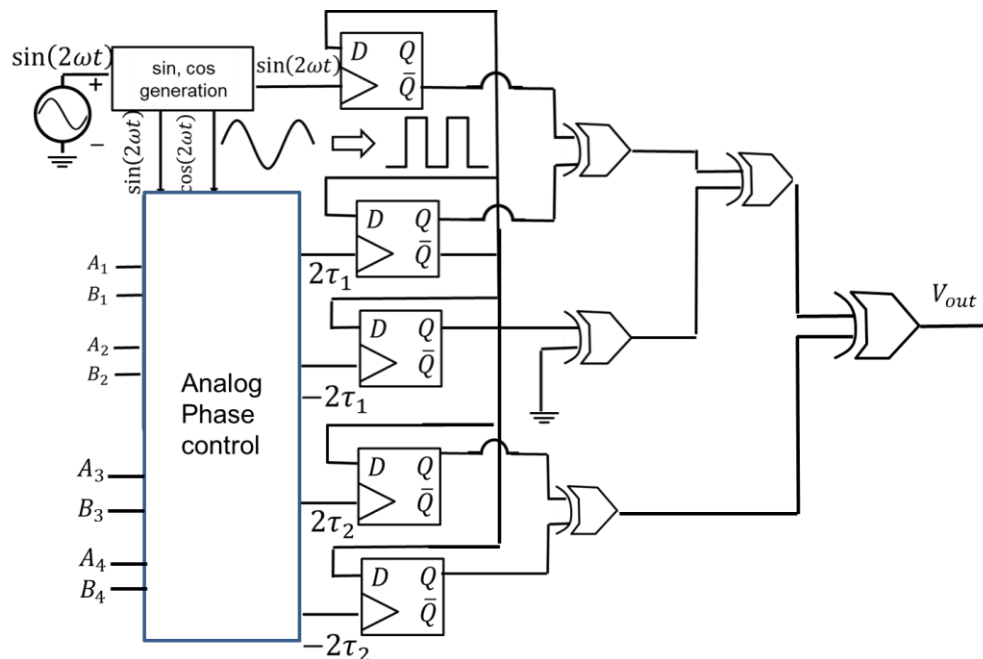
HD3 & HD5 Suppression Simulation

Parameters

$$T/2 = 5 [\mu s], 2\tau_1 = 0.92578 [\mu s], 2\tau_2 = 0.656805 [\mu s]$$

$$c_1 = 1, c_2 = -0.1, c_3 = -0.05, c_4 = -0.01, c_5 = -0.005$$

$$\frac{b_1}{a_1} = \frac{489}{235}, \frac{b_2}{a_2} = \frac{313}{122}, \frac{b_3}{a_3} = \frac{938}{868}, \frac{b_4}{a_4} = \frac{929}{868}$$



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Conclusion

Summary

- We proposed low-distortion signal method using analog phase shift & rectangular.

Digital ATE + Simple analog circuit & BOST



No need expensive signal generator

Future task

- Consideration of delay time & threshold voltage of Flip-Flop
- It is necessary to verify with the actual circuit